### 5.2 Properties of Functions

* In a relation, the set of the first elements are called the domain ; the set of the second elements are called the range.
*A function is a relation where each element of the domain is associated with exactly one element of the range.
ex.

ex.



* The domain represents the set of input values. The range represents the set of output values. On the cartesian plane, the values on the $y$-axis depend on the input values on the x-axis. Thus, the input values are independent of the output values.
* For functions with numeric values, we use formulas ex. area of a disc
$A(r)=2 \pi r^{2}+2 \pi r h$

$A(r)=2 \pi r^{2}+2 \pi r(2)$
$A(r)=2 \pi r^{2}+4 \pi r$
$A(r)=2 \pi r(r+2)$
let $r=6 \mathrm{~cm}$

$$
A(6)=2 \pi(6)(6+2)
$$


does not mean $A \times r$ it means Area (A) is a function
radius $(r) \Rightarrow$ in orther wordo

$$
\text { "Find Area when } r=6 \text { " }
$$ Area depends on

$$
A(6)=12 \pi(8)
$$ radio

$$
\begin{aligned}
& A(6)=96 \pi \text { unis }^{2} \\
& A(6)
\end{aligned}
$$

$$
e x / / h(t)=-4.9 t^{2}+3 t+1
$$

ex. The equation $V=-0.08 d+50$ represents the volume,
$V$ litres, of gas remaining in a vehicle's tank after travelling $d$ kilometres. The gas tank is not refilled until it is empty.
a) Describe the function. a car has a sol tank and Write the equation in function notation. burns 0.08 L/KMn
b) Determine the value of $V(600)$. What does this number represent?

$$
\triangleright V(d)=-0.08 d+50
$$

$$
\text { Determine the value of } d \text { when } V(d)=26 . \quad \triangleleft b) V(600)=-0.08(600)+50
$$

c) Determine the value of $d$ when $V(d)=26$.

## What does this number represent?

$\rightarrow$ when the vohme $=261$,
how far have we driven? $\rightarrow V(d)=-0.08 d+50$
$\begin{array}{r}26 \\ -50\end{array}=-0.08 d+50-50$
$\frac{-24}{-0.08}=\frac{-0.08 d}{-0.08} \Rightarrow A=300 \mathrm{~km}$

## CHECK YOUR UNDERSTANDING

3. The equation $C=25 n+1000$ represents the cost, $C$ dollars, for a feast following an Arctic sports competition, where $n$ is the number of people attending.
a) Describe the function.

Write the equation in function notation.
a) $C(n)=25 n+1000$

The wot is $25^{\$ / p e r o o n}$
$t$ a fixed fee of $\$ 1000$
b) Determine the value of $C(100)$. What does this number represent?
c) Determine the value of $n$ when $C(n)=5000$. What does this number represent?
b) $C(100)=25(100)+1000$ $=2500+1000$ $=3500 \$$
c) How many can attend on a budget of $\$ 5000$ ? $5000=25 n+1000$
$-1000 \quad-1000$

## Quiz in 2 days

Homefun: Pg. 270 \# 4-6, 9-12, 14-17, 19-23 + Assess your Understanding Pg. 275

$$
\frac{4000}{25}=\frac{25 n}{25}
$$

$$
160=n
$$

