

5.5 Graphs of Functions and Relations

* The **domain** of a function is the set of values attributed to the **independent** variable (the horizontal axis).

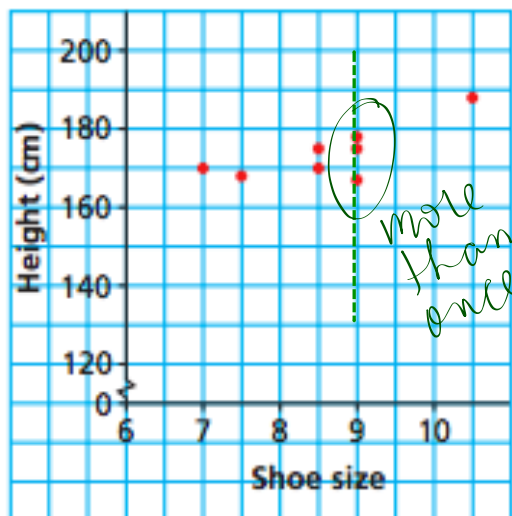
* The **range** of a function is the set of values attributed to the **dependent** variable (the vertical axis).

* When the domain of a function is restricted to a set of **discrete** values, the points on its graph are **not connected**.

* The Vertical Line Test (VLT): when considering the graph of a **function** the VLT will be satisfied. To satisfy the VLT, a **vertical line** will never cross/touch the graph of the function at **more than one point**.

ex. Determine the domain and range and indicate whether each is a function or not.

a) Height against Shoe Size

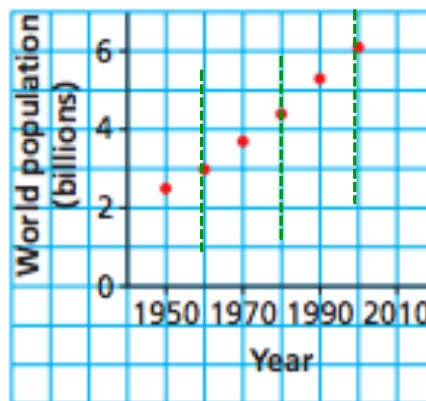


Not a function
 \Rightarrow fails the VLT

$$D: \{7, 7.5, 8.5, 9, 10.5\}$$

$$R: \{167, 168, 170, 175, 178, 188\}$$

b) World Population



Function \Rightarrow passes the VLT

$$D: \{1950, 1960, 1970, 1980, 1990, 2000\}$$

$$R: \{2.5, 3, 3.7, 4.3, 5.2, 6\}$$

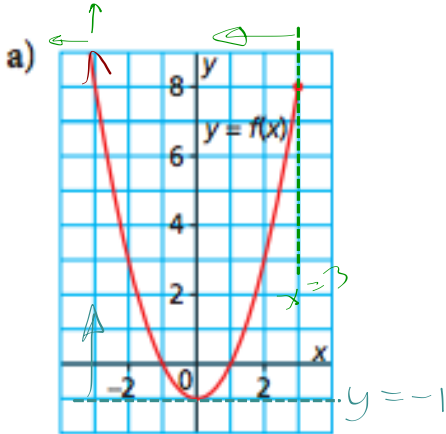
inputs \rightarrow

outputs \rightarrow

can't be divided \rightarrow

we could use a dotted line \rightarrow

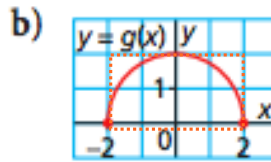
ex. Determine the domain and range of the graph of each function.



$D = \{x \in \mathbb{R} \mid x \leq 3\}$

"is an element of" → "real number set"
 "whereby" → "since the curve is continuous"

$R = \{y \in \mathbb{R} \mid y \geq -1\}$



solid endpoints

$D: \{x \in \mathbb{R} \mid -2 \leq x \leq 2\}$

$R: \{y \in \mathbb{R} \mid 0 \leq y \leq 2\}$

ex. Here is a graph of the function $f(x) = -3x + 7$.

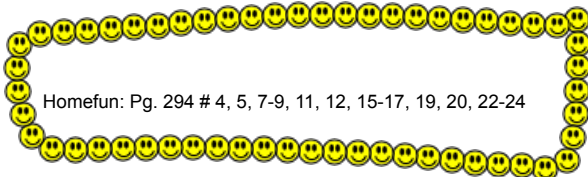
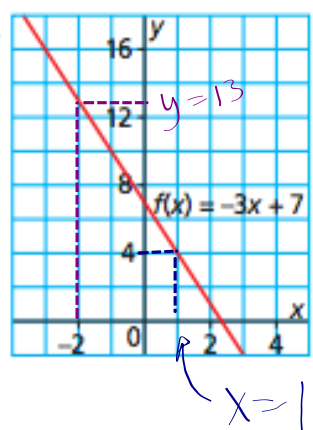
a) Determine the range value when the domain value is -2.

$y = -3x + 7$

$y = 13$

b) Determine the domain value when the range value is 4.

$x = 1$



5.1-5.5 → Tuesday

Quiz tomorrow