

15. ① $Ax + By = C$

② $Dx + Ey = F$

if (x_0) is a solⁿ

if $(0, y)$ is a solⁿ

① $A(0) + \frac{By}{B} = \frac{C}{B}$

$$y = \frac{C}{B}$$

② $\frac{D(0)}{E} + \frac{Ey}{E} = \frac{F}{E}$

$$y = \frac{F}{E}$$

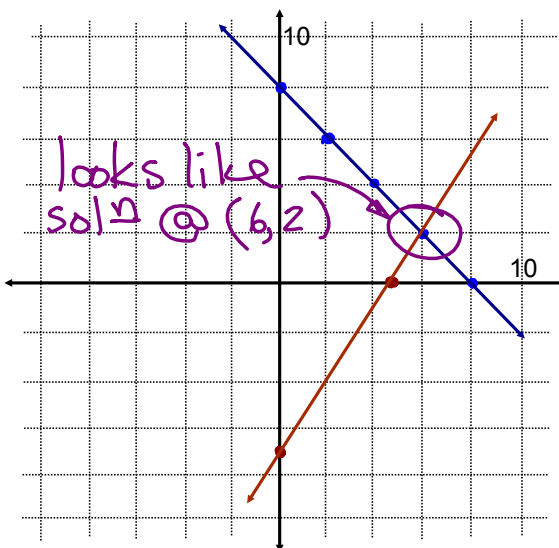
$$\therefore \frac{C}{B} = \frac{F}{E}$$

7.2 Solving Systems Graphically

* The **solution** of a system of equations is the **point of intersection** of the two graphs. This coordinate satisfies both equations at the same time.

ex. Graphically solve the the following system:

$$\begin{cases} x + y = 8 & \textcircled{1} \\ 3x - 2y = 14 & \textcircled{2} \end{cases}$$



① $y = -x + 8$ ← y-int.
 $m = -1$

② y-int: $x = 0$
 $3(0) - 2y = 14$
 $-2y = 14$
 $y = -7$

③ x-int: $y = 0$
 $3x - 2(0) = 14$
 $3x = 14$
 $x = 14/3$
 ≈ 4.6

Test the solution in equation ① & ②

$$x = 6 \quad \hat{=} \quad y = 2$$

① $x + y = 8$
 $6 + 2 = 8$ ✓
 satisfies equⁿ ①

② $3x - 2y = 14$
 $3(6) - 2(2) = 14$
 $18 - 4 = 14$
 $14 = 14$ ✓

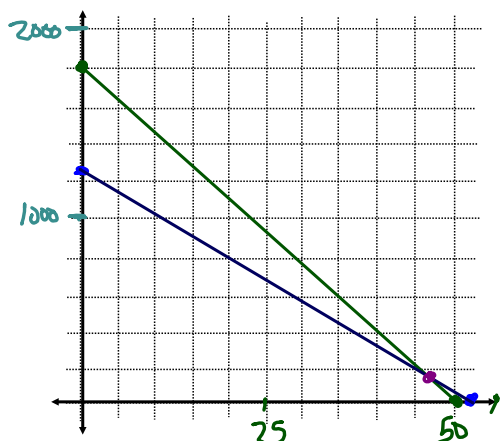
satisfies equⁿ ②

∴ (6, 2) is definitely the pt. of intersection

ex. A box of 36 golf balls has a mass of 1806 g. If we remove 12 balls, the box has a mass of 1254 g. What is the mass of one ball? How much does the empty box weigh?

let x = the mass of one ball

y = the mass of the box



looks like $(46, 180)$

$$\textcircled{1} \quad 36x + y = 1806$$

$$x\text{-int: } y = 0$$

$$\frac{36x}{36} = \frac{1806}{36}$$

$$x = 50.16$$

$$y\text{-int: } x = 0$$

$$36x + y = 1806$$

$$y = 1806$$

$$\textcircled{2} \quad 24x + y = 1254$$

$$x\text{-int: } y = 0$$

$$\frac{24x}{24} = \frac{1254}{24}$$

$$x = 52.25$$

$$y\text{-int: } x = 0$$

$$y = 1254$$

Test the solution in equation $\textcircled{1}$ & $\textcircled{2}$

test $(46, 180)$

$$\textcircled{1} \quad 36(46) + 180$$

$$= 1836$$

$\neq 1806$ but is close

$$\textcircled{2} \quad 24(46) + 180$$

$$= 1284$$

$$\neq 1254$$

∴ The golf ball weighs about 46g and the box weighs around 180g (180g would be a better estimate)